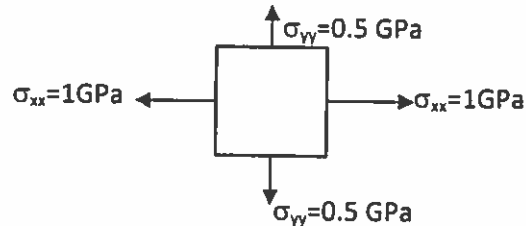


**PLEASE NOTE: Answer all 3 problems.**

**Problem #1**

A thin plate, shown in the figure, is subjected to biaxial stress field of  $\sigma_{xx}=1\text{GPa}$  and  $\sigma_{yy}=0.5\text{GPa}$ .



1. Calculate the strains in the x, y directions if the plate is made of steel
2. Calculate the strains in the x, y directions if the plate is made of  $0^\circ$  unidirectional 60 vol% carbon fiber reinforced epoxy composite and the fibers are oriented in the x-direction
3. Calculate the strains in the 1,2 directions (1 direction is parallel to the fiber axis, 2 direction is normal to the fiber axis but in-plane) if the plate is made of a  $45^\circ$  unidirectional 60 vol% carbon fiber reinforced epoxy composite
4. Show in a simple 2-D schematic how the plate will deform as a result of the applied stress field for each of the three cases i.e, steel plate,  $0^\circ$  unidirectional and  $45^\circ$  unidirectional carbon fiber reinforced epoxy composites
5. What is the definition of
  - a) an isotropic material
  - b) orthotropic material
  - c) anisotropic

List and justify your assumptions

**DATA GIVEN**

| Material | Modulus (GPa) | Poisson's ratio |
|----------|---------------|-----------------|
| steel    | 207           | 0.33            |
| epoxy    | 3.6           | 0.35            |
| fiber    | 220           | 0.2             |

$G_{12}=3.254\text{GPa}$

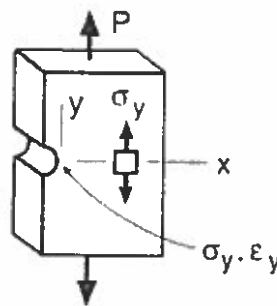
$\nu_{12}$  calculated using the rule of mixtures

$\nu_{21}=\nu_{12} E_{22}/E_{11}$ , where  $E_{11}$  and  $E_{22}$  are the longitudinal and transverse modulus of the plate

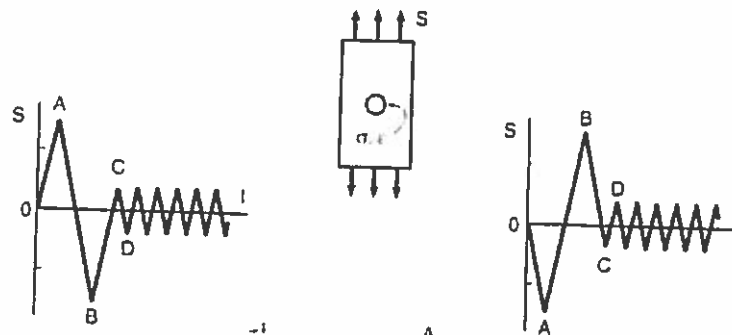
$V_f = 60\%$  (volume fraction of the fibers)

**Problem # 2:**

- 1) Consider the notched member shown below. Assume it is loaded sufficiently for local yielding to occur, and then completely unloaded ( $P = 0$ ). For this loading scenario:
  - a. plot a schematic of the nominal stress,  $S$  ( $S = P/A$  with  $A$  being the gross cross-section area) as a function of local strain at the notch root,  $\epsilon_y$ ;
  - b. plot a schematic of the local stress at the notch root,  $\sigma_y$ , versus  $\epsilon_y$ ;
  - c. discuss how these plots (a and b) could be obtained in a more quantitative manner;
  - d. Upon unloading ( $P = 0$ ), plot a schematic of the normal stress,  $\sigma_y$ , as a function of distance  $x$  from the notch root.



- 2) Consider a similar notched member (see image below) for which two different load histories are applied (see left and right plots of nominal stress,  $S$ , versus time).
  - a. For each load history, plot a schematic of the local stress versus local strain at the notch root (assume the first cycle promotes significant plastic deformation at the notch).
  - b. Which load history should result in a longer fatigue life and why (assume that the low amplitude cycling continues until failure of the component)?
  - c. How would you estimate the fatigue life for this notched member for each load configuration? List your main assumptions.



### Problem #3

Consider a 6-bar truss structure as shown in Figure 1. All the bars in the truss have the same cross-sectional area of  $A$ . Bars  $AB$  and  $CD$  are made of linear elastic materials, which are characterized by Young's moduli  $E_1$  and  $E_2$  and coefficients of thermal expansion  $\alpha_1$  and  $\alpha_2$ . All the other bars are considered to be rigid with zero coefficient of thermal expansion. The structure is initially stress-free.

- Determine the stress developed in each bar due to a small, uniform temperature increase  $\Delta T$  throughout the entire structure.
- How would your answer to (a) change if the structure is simultaneously subjected to the above thermal loading and a pair of compressive forces of magnitude  $F$  on joints  $A$  and  $B$ ?

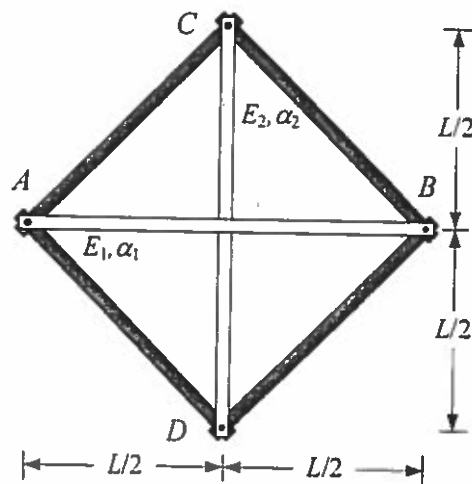


Figure 1